Neutron stars in the framework of Landau's theory

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A general formula of the symmetry energy for many-body interaction is proposed and the commonly used two-body interaction symmetry energy is recovered. Within Landau's theory (Lt), we generalize two equations of state (EoS) CCS δ 3 and CCS δ 5 to asymmetric nuclear matter. We assume that the density and density difference between protons and neutrons divided by their sum are order parameters. We use different EoS to study neutron stars by solving the TOV equations. We demonstrate that different EoS give different mass and radius relation for neutron stars even when they have exactly the same ground state (gs) properties (E/A, ρ_0 , K, S, L and K_{sym}). Furthermore, for one EoS we change K_{sym} and fix all the other gs parameters. We find that for some K_{sym} the EoS becomes unstable at high density even for neutron matter. This suggests that a neutron star (NS) can exist below and above the instability region but in different states: a quark gluon plasma (QGP) at high density and baryonic matter at low density [1].

We fix incompressibility K=225 MeV, symmetry energy S=28.5 MeV, and the slope of symmetry energy L=73 MeV from Skyrme EoS CK225₁ [1]. In this case, EoS CK225₁, CK225 and CCS δ 3 have the same values for K, S, L and K_{sym}. This motivates us to fix the same values of S, L and K_{sym} for EoS CCS δ 5. For the four EoS, CK225₁, CK225, CCS δ 3 and CCS δ 5, we solve the TOV equations for the PNM to obtain the mass-radius relation of neutron stars. The results are shown in Fig. 1.



FIG. 1. The NS mass-radius relation for CK225₁, CK225, CCS δ 3 and CCS δ 5 with same values of K=225 MeV, S=28.5 MeV, L=73 MeV and K_{svm} = -25 MeV.

We can see that the mass-radius relations for the neutron stars are different for the four EoS (CK225₁ and CK225 are the same in this case) even though they have the same values of K, S, L and K_{sym}. This indicates that the mass-radius relation of the NS is not only determined by K, S, L and K_{sym}, but the high density dependence of the EoS is crucial. We also notice that there are wiggles in the mass-radius relation of PNM NS for CCSδ3 and CCSδ5 rather than CK225₁ and CK225 because of a cross-over at high density for the two EoS. Thus, the second order PT assumed in deriving CCSδ3 and CCSδ5 becomes cross-over for these parameters choice. The maximum mass of the NS for CCSδ3 is larger than the one for CK225₁ or CK225. The reason for this is because of the higher power of ρ in CCSδ3 compared to CK225. But the maximum mass of the NS for CCSδ5 (which contains even higher power density values) is lower than the one for CCSδ3. The 'missed phase transition' or cross-over softens the EoS and causes the pressure for CCSδ5 to decrease compared to the one for CCSδ3 at the same density.

The EoS CCS δ 5 displays an instability when K_{sym}=-215MeV corresponding to a first order PT. In this case the TOV equations cannot be solved in the instability region. We have used the Maxwell construction to determine the densities where the two phases (which we call phase A and B) are separated. In Fig. 2, we plot the results obtained solving the TOV equations when the central density is $10\rho_{0}$.



FIG. 2. The density profiles of a neutron star with central density $10\rho_0$ for EoS CCS δ 5 when S = 28.5 MeV, L = 50 MeV and Ksym = -215 MeV. The red lines are the Maxwell construction in the instability region.

[1] H. Zhang, J. Sahagun, and A. Bonasera, arXiv: 1411.3030.